

# Investigating a Physically- Based Signal Power Model for Robust Low Power Wireless Link Simulation

TAL RUSAK

tr76@cornell.edu

Department of  
Computer Science  
Cornell University

PHILIP LEVIS

pal@cs.stanford.edu

Computer Systems  
Laboratory  
Stanford University

# Outline

---

- **Introduction**
- Phase correction and signal extrapolation
- Validation and Evaluation
- Conclusion

# Low Power Wireless Link Performance Is Poor

- Protocols for sensor networks are carefully designed and heavily simulated
- Packet yield in real deployments is low:
  - Volcano Study: 68% [ESWN 05]
  - Great Duck Island: 58% [SenSys 04]
  - Redwood Study: 40% [SenSys 05]
  - Potato Agriculture Study: 2% [WPDRTS 06]
- Low packet yield leads to loss of information from networks

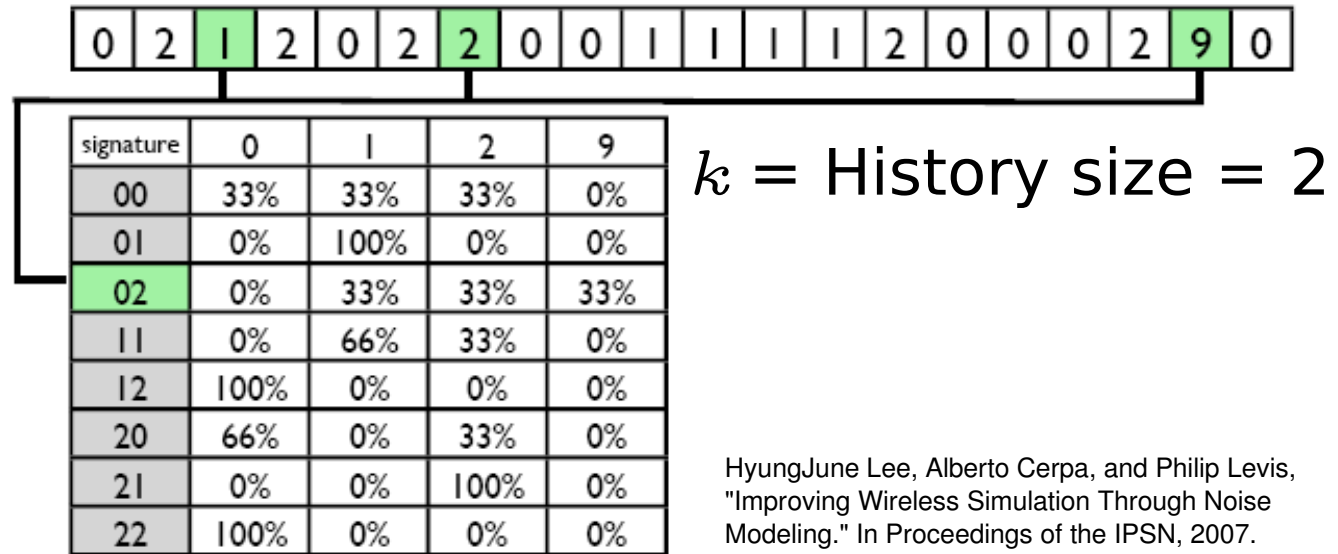
# Wireless Link Simulation

- Analytical Models
  - For example, Path Loss and Shadowing Model [ICEE 06]
  - Many assume packet reception independence
- Empirical Models
  - Packet receptions and losses are *not* temporally independent
  - Noise+Interference modeled using CPM [IPSN 07]

# TOSSIM 2.0.1 (2007)

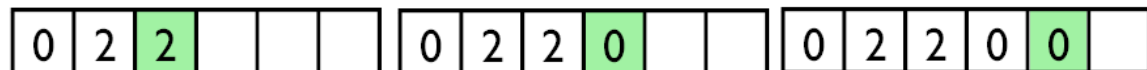
- Closest Fit Pattern Matching (CFPM):

- (1) Pre-process an experimental noise trace:



- (2) Take  $k$  values from experiment; then sample

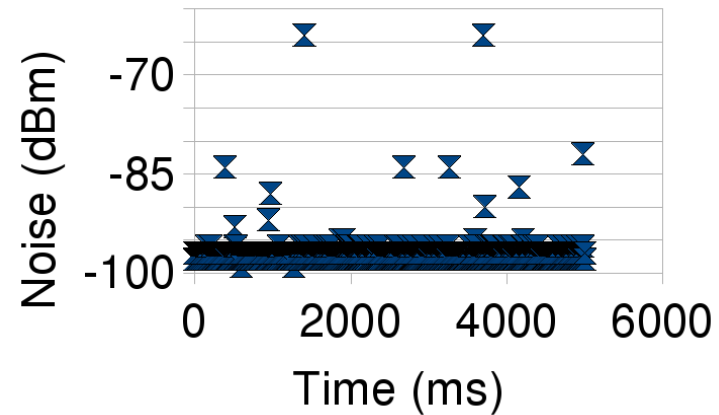
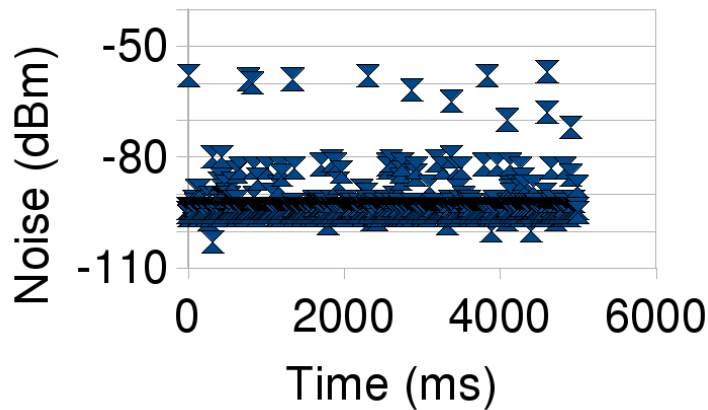
PMF:



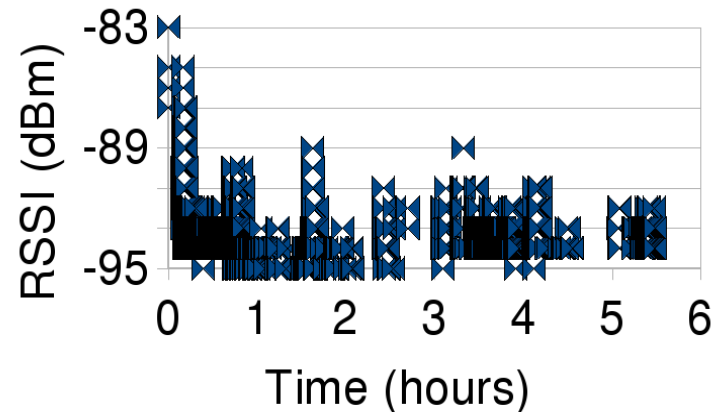
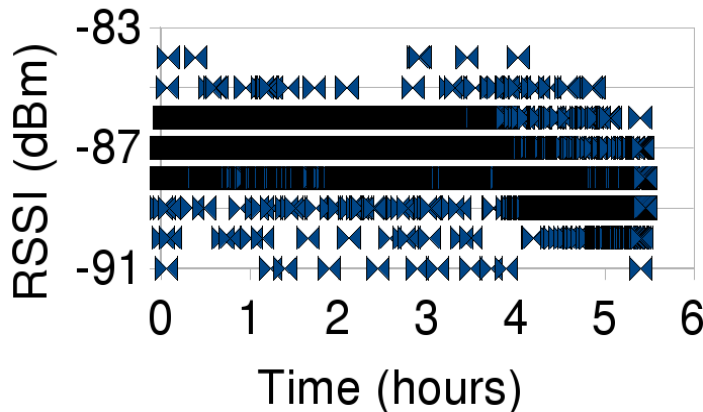
- Signal power given by constant link gain value.

# Reasons for Packet Reception Correlation

- Noise+Interference in environment is correlated



- Signal Power of successive packets is also correlated



# Physically Modeling Signal Power

---

- **Idea:** Collect a signal power trace and use CPM to model signal power.
- Collecting power traces is more complex than collecting noise traces, since:
  - Signal power is a property of a pair of nodes in the network
  - Signal power can only be approximated by sampling the RSSI register, which actually reports signal+noise, where wave phases are considered
  - If a packet is lost in transmission, then even the RSSI estimate is not possible.

# Contributions

- We suggest solutions to major challenges in modeling signal power:
  - Correcting for phase
  - Two algorithms for extrapolating from lossy traces: Average Value and Expected Value
- Our algorithms improve simulation substantially:
  - PRR simulated to within 22% absolute difference
  - Methods reduce KW distance of simulations by 66% compared to current approaches



# Outline

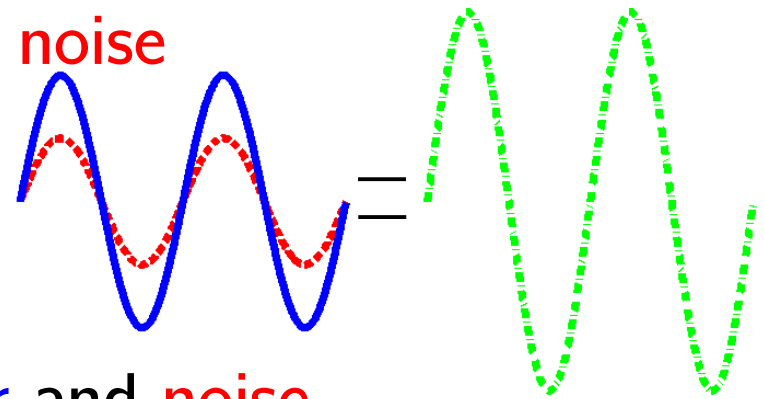
---

- Introduction
- Phase correction and signal extrapolation
- Validation and Evaluation
- Conclusion

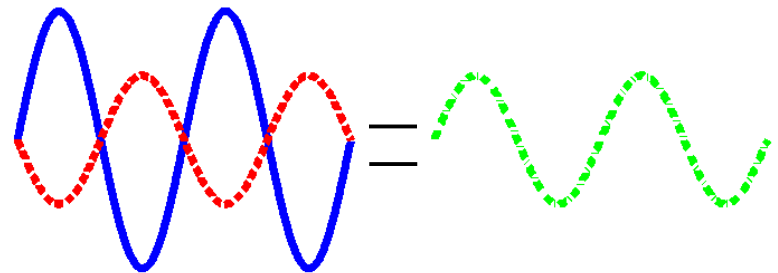
# Converting RSSI Readings to Signal Power

- Phase assumption used to correct RSSI reading:

- In phase **signal power** and **noise**



- Out of phase **signal power** and **noise**



- Neutral phase: assumes net phases cancel out

- These assumptions are simplifications to reality.

# Algorithm for Filling-In Lossy Signal Power Links

- Two algorithms suggested:
  - Fill in average value for all missing values
  - Compute expected distribution of missing signal power values over the whole trace and then sample the distribution

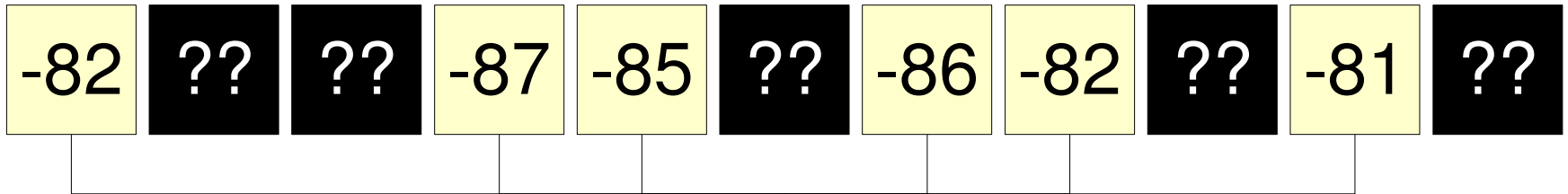
# Average Value Filling-In Algorithm

Lossy Signal Power (dBm) =



# Average Value Filling-In Algorithm

Lossy Signal Power (dBm) =

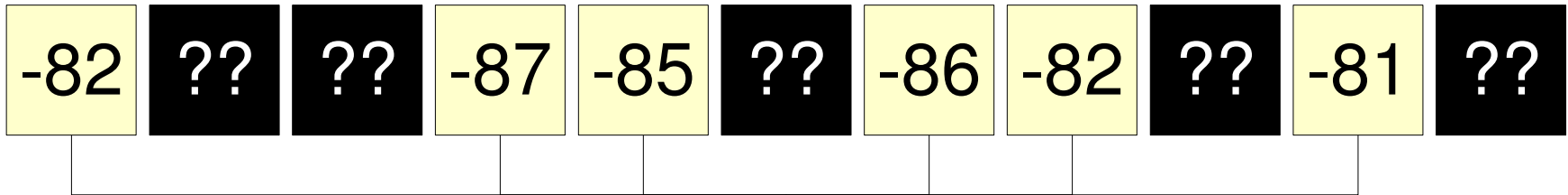


Average Signal Power  
(Rounded to Integer)  
(dBm) =

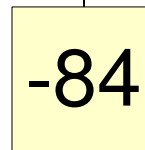
-84

# Average Value Filling-In Algorithm

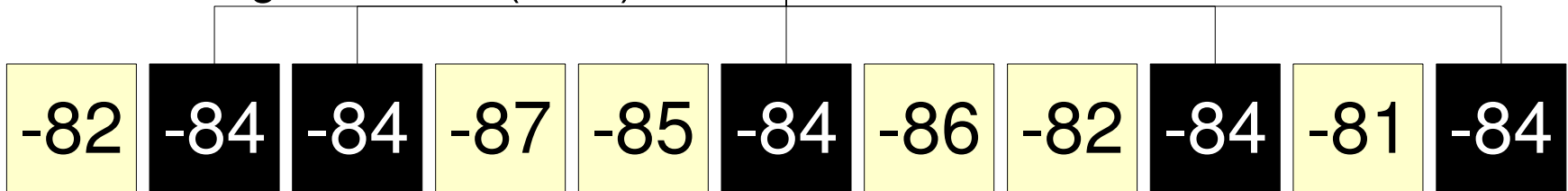
Lossy Signal Power (dBm) =



Average Signal Power  
(Rounded to Integer)  
(dBm) =



Filled-In Signal Power (dBm) =



# Expected Value PMF Filling-In Algorithm

Average Noise (dBm) = -90

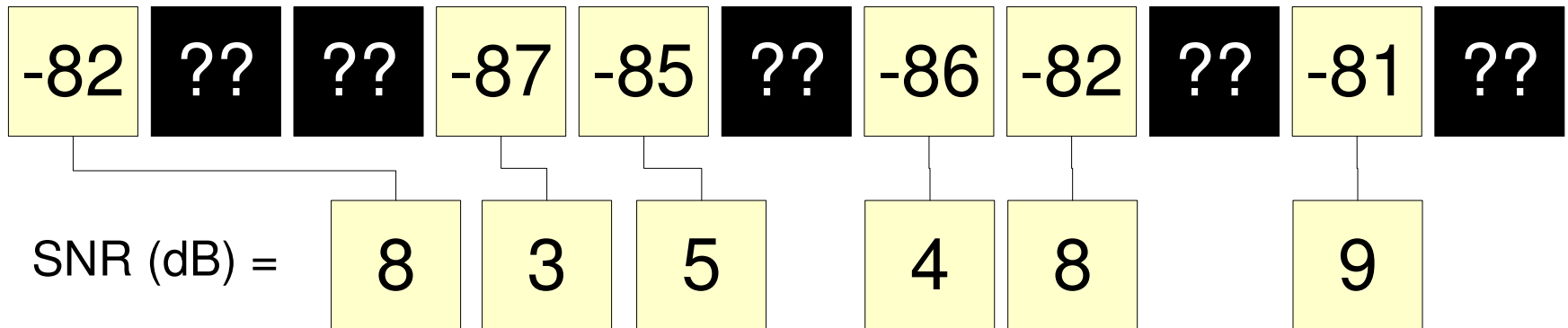
Lossy Signal Power (dBm) =



# Expected Value PMF Filling-In Algorithm

Average Noise (dBm) = -90

Lossy Signal Power (dBm) =

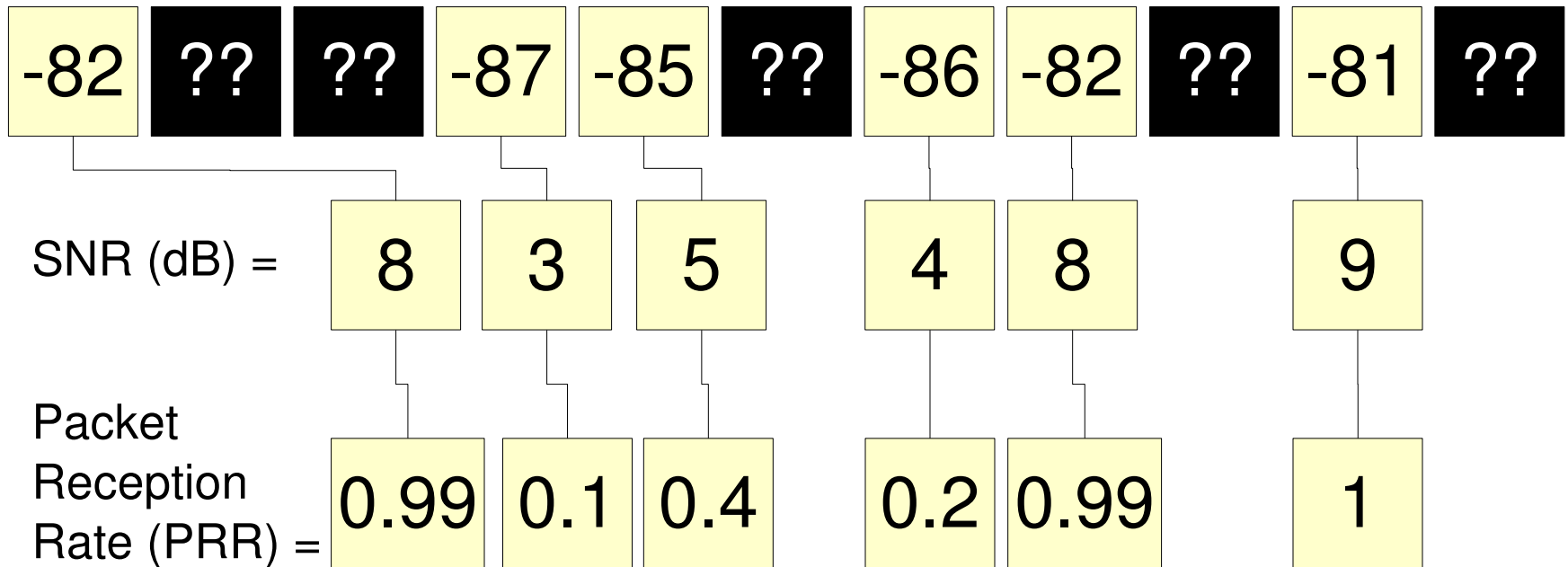




# Expected Value PMF Filling-In Algorithm

Average Noise (dBm) = -90

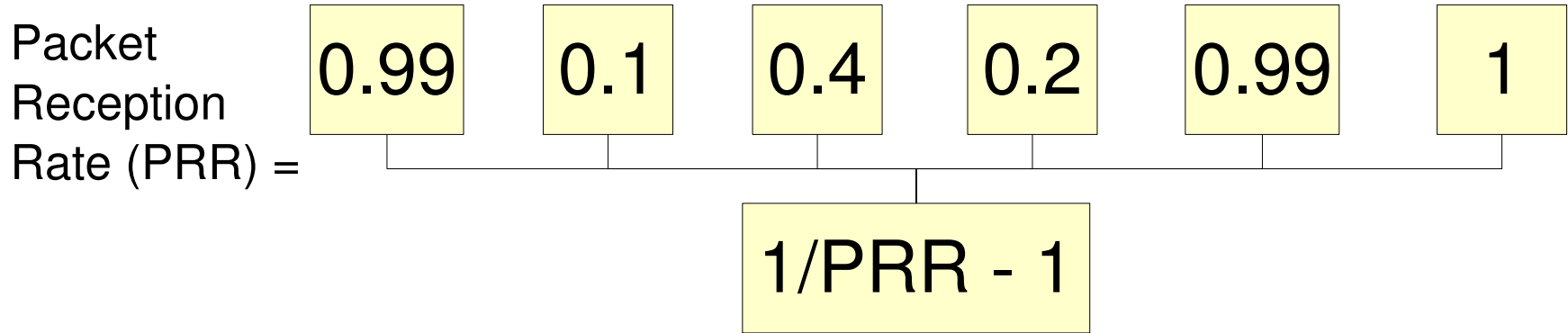
Lossy Signal Power (dBm) =



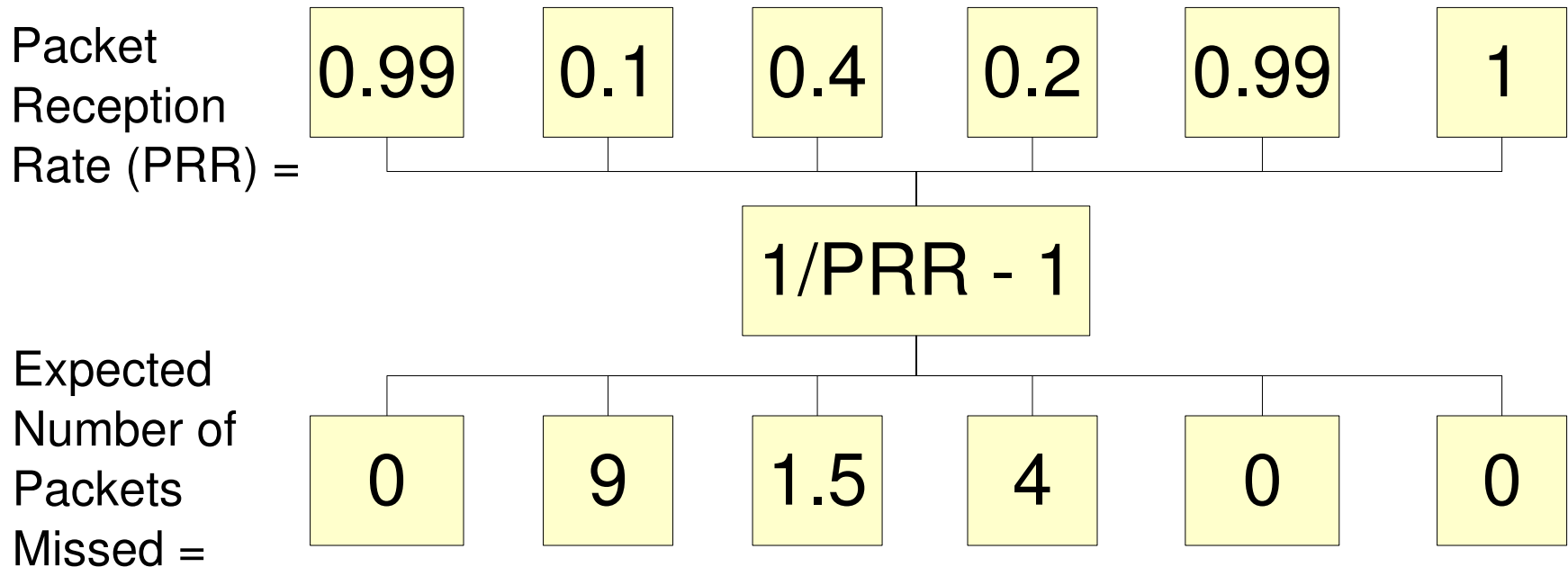
# Expected Value PMF Filling-In Algorithm (continued)

Packet Reception Rate (PRR) =	0.99	0.1	0.4	0.2	0.99	1
-------------------------------------	------	-----	-----	-----	------	---

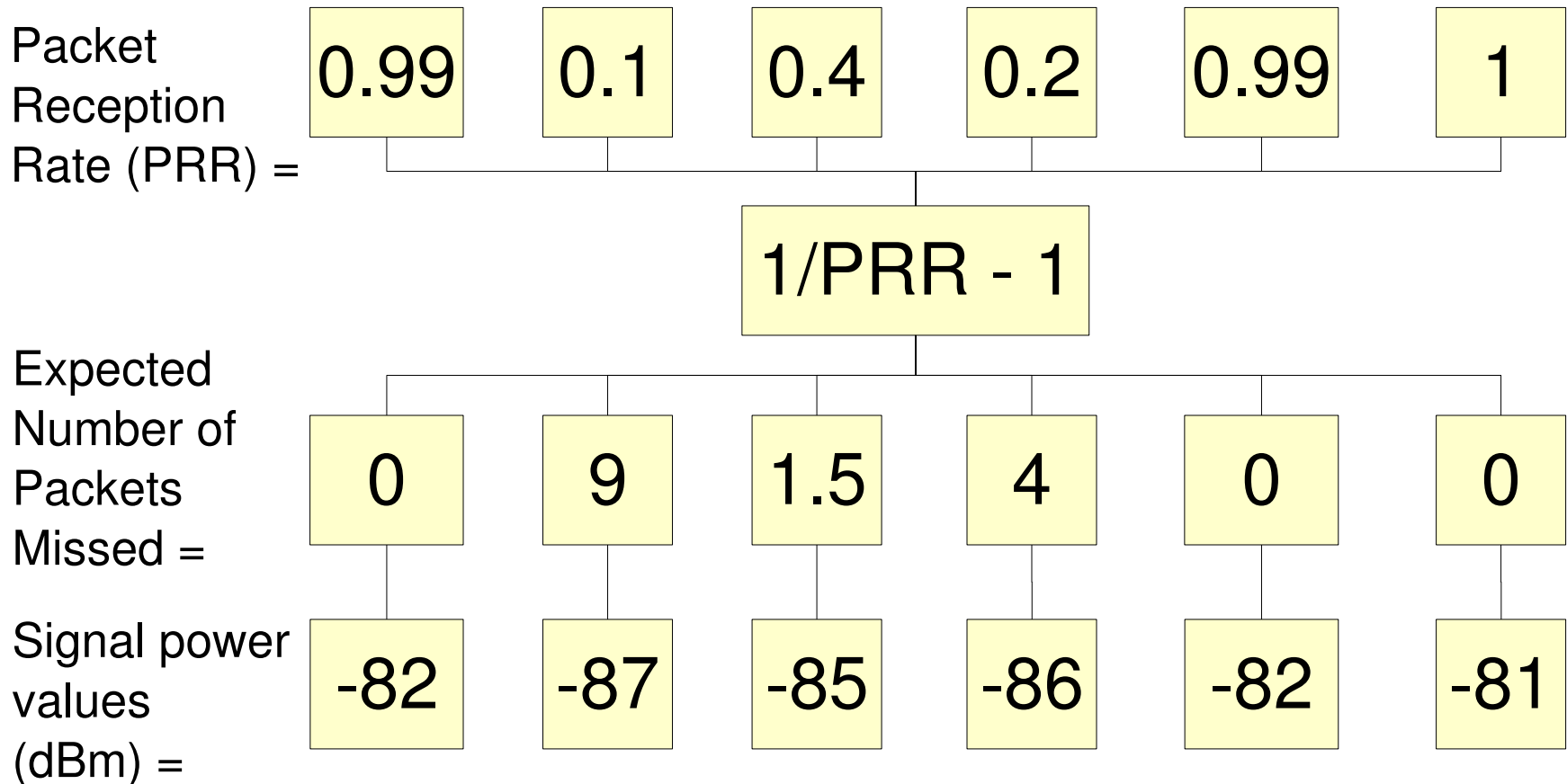
# Expected Value PMF Filling-In Algorithm (continued)



# Expected Value PMF Filling-In Algorithm (continued)

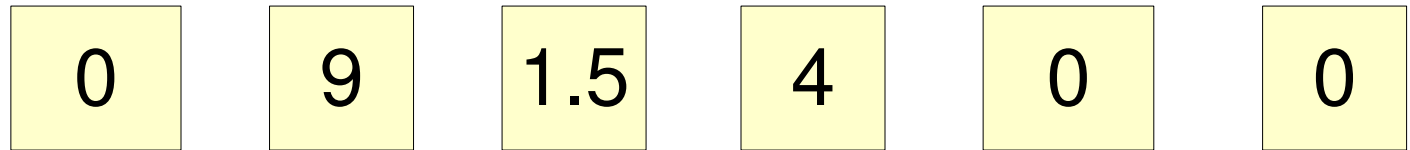


# Expected Value PMF Filling-In Algorithm (continued)

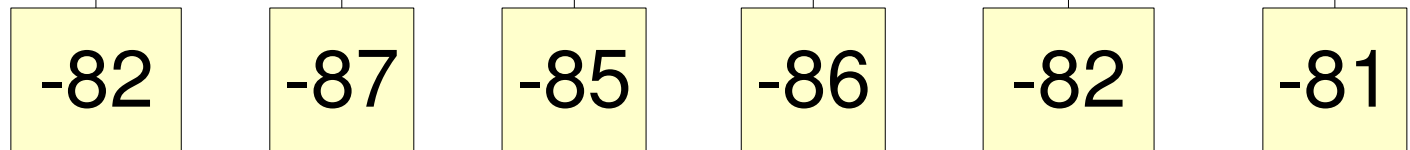


# Expected Value PMF Filling-In Algorithm (continued)

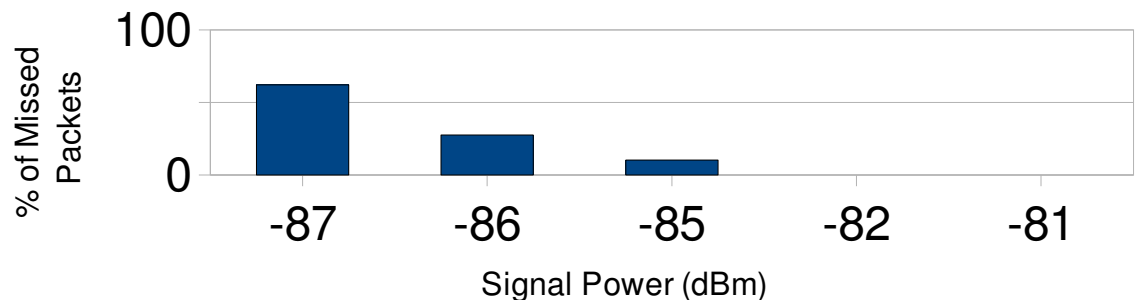
Expected  
Number of  
Packets  
Missed =



Signal power  
values  
(dBm) =

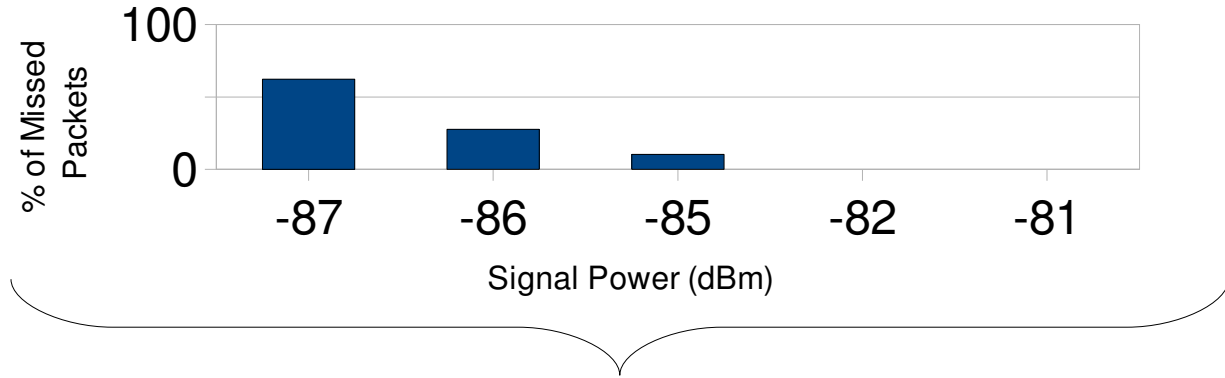


Expected  
Packets PMF =



# Expected Value PMF Filling-In Algorithm (continued)

Expected  
Packets PMF =



Filled-In Signal Power (dBm) =



# Outline

---

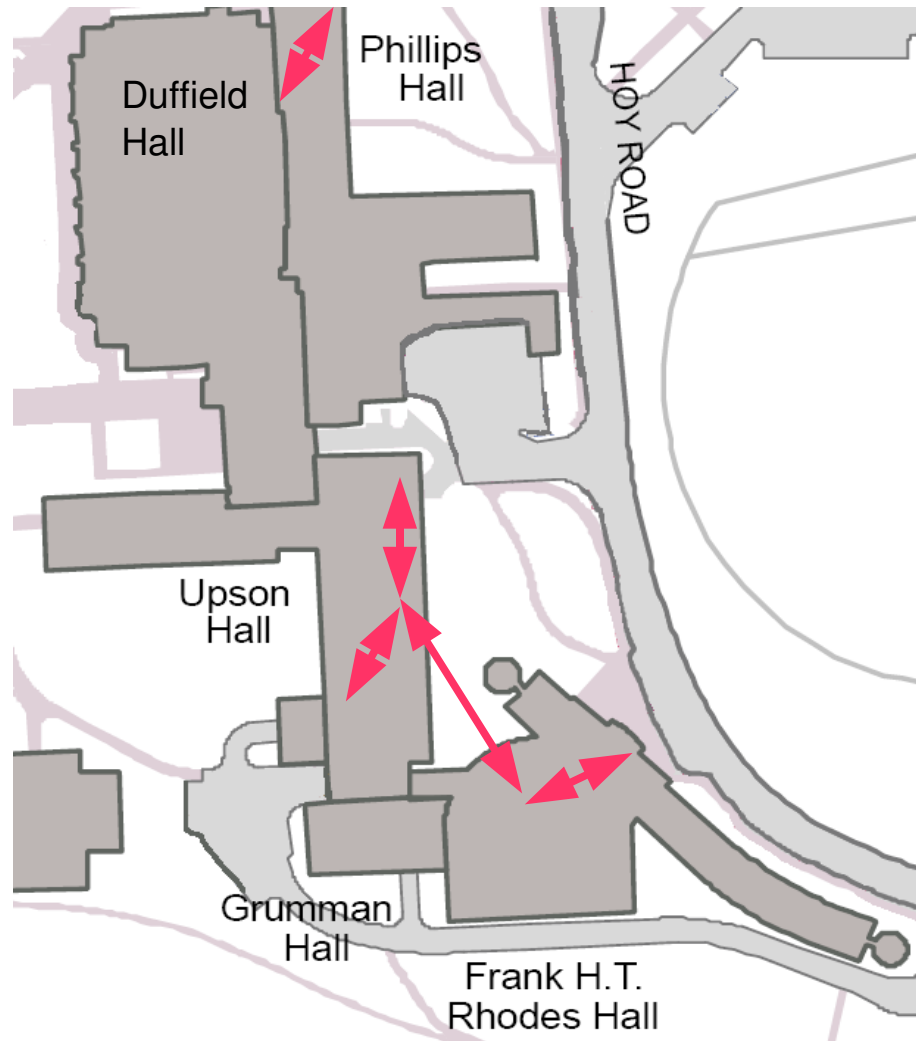
- Introduction
- Phase correction and signal extrapolation
- **Validation and Evaluation**
- Conclusion



# Validation

- Goal is to correctly simulate a particular link between to nodes
- It is possible to use experiments to validate this simulation method
- Conducted packet delivery experiments at 4 Hz for 12 hours at various locations on the Cornell University Campus.
- 4 Hz frequency chosen as a baseline: future work will investigate different collection frequencies and the impacts on the results.

# Experiment Locations



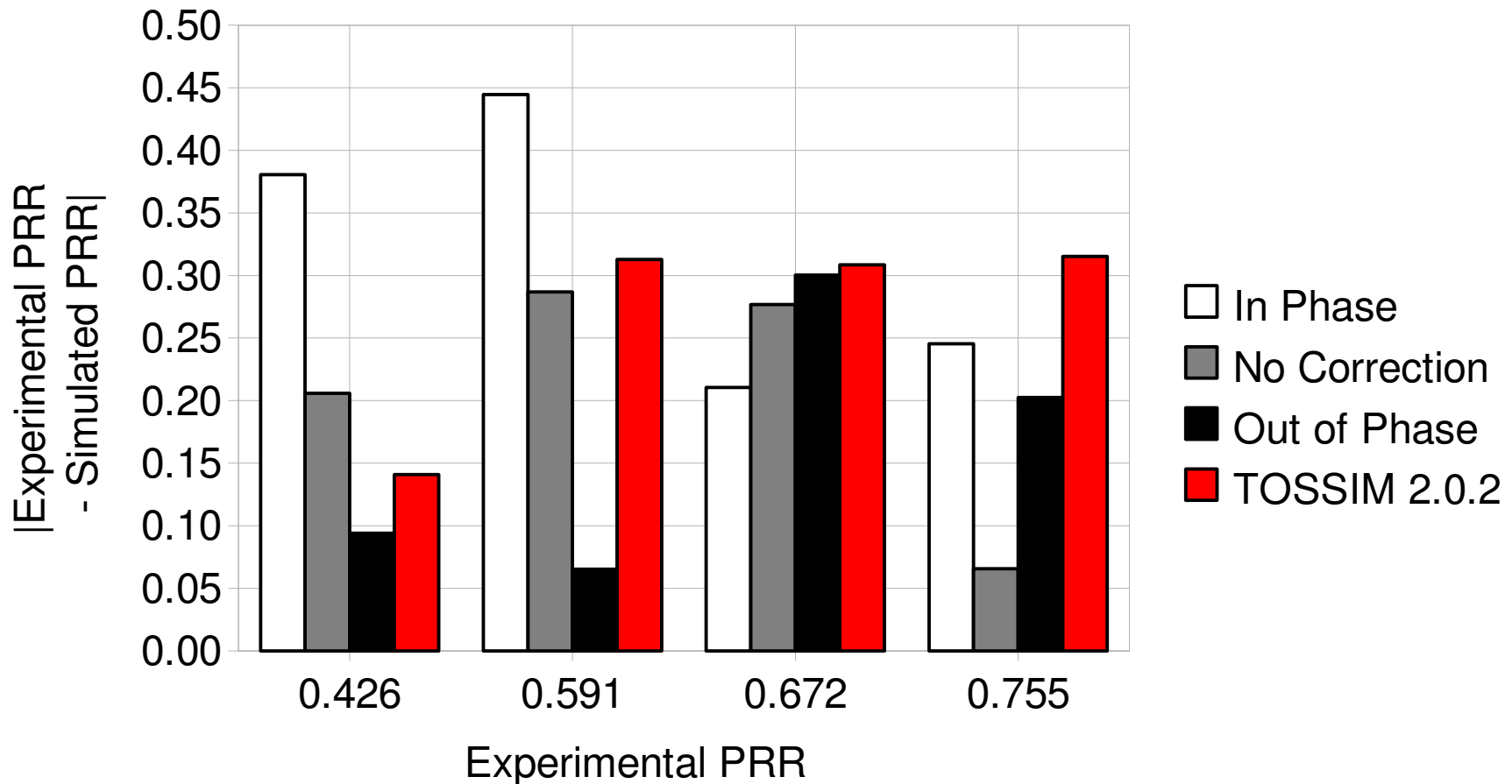
# Evaluation Criteria

---

- Packet Reception Rate (PRR)
  - First order parameter, difficult to get right in general wireless simulators
- Kantorovich-Wasserstein (KW) distance on Conditional Packet Delivery Functions (CPDFs)
  - Rigorous measure of the similarity between two distributions, which places more emphasis on rare rather than common case
  - Captures packet burstiness at the level of individual packets.

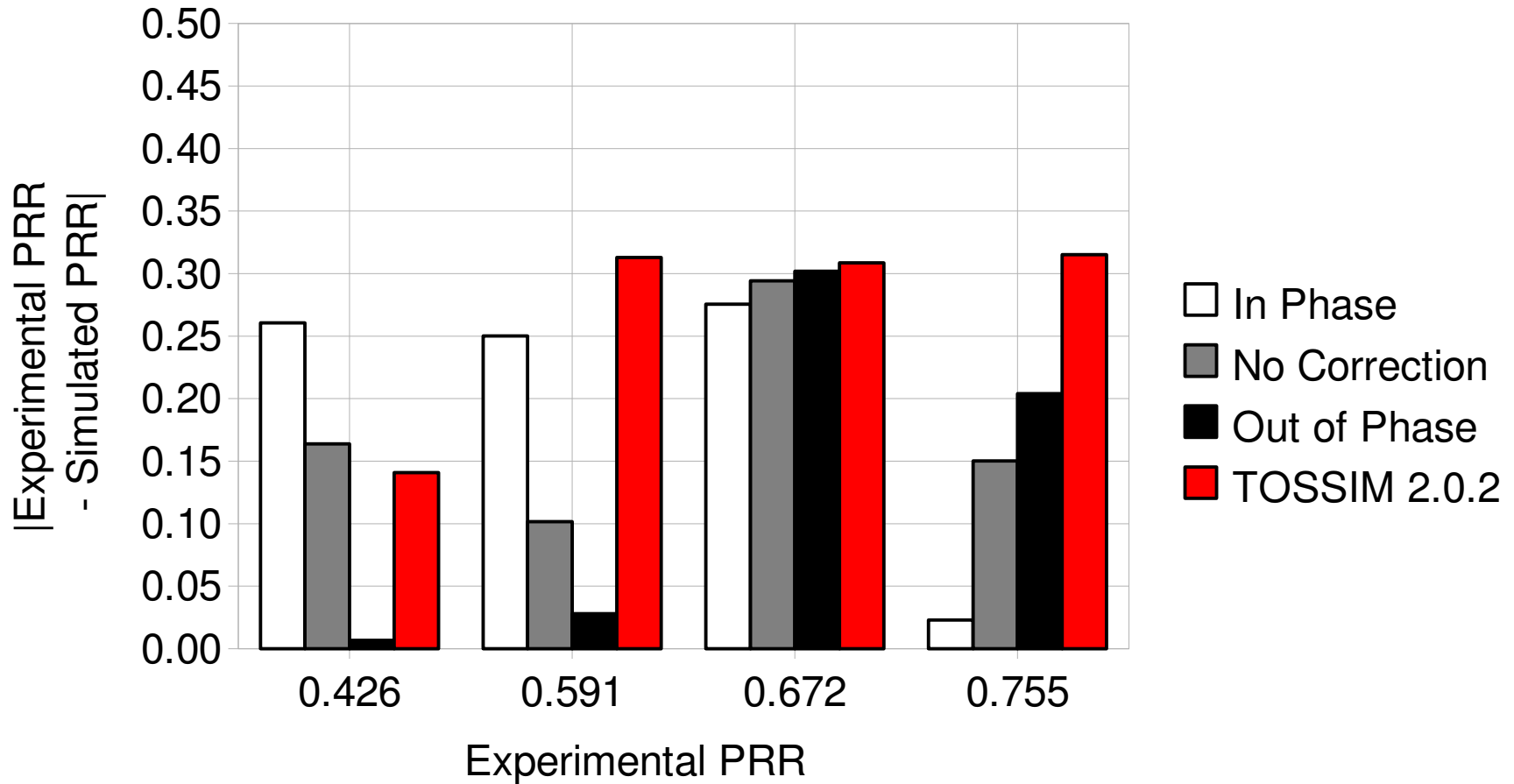
# PRR for Expected Value PMF Algorithm

- Maximum absolute error bounded by 22%.



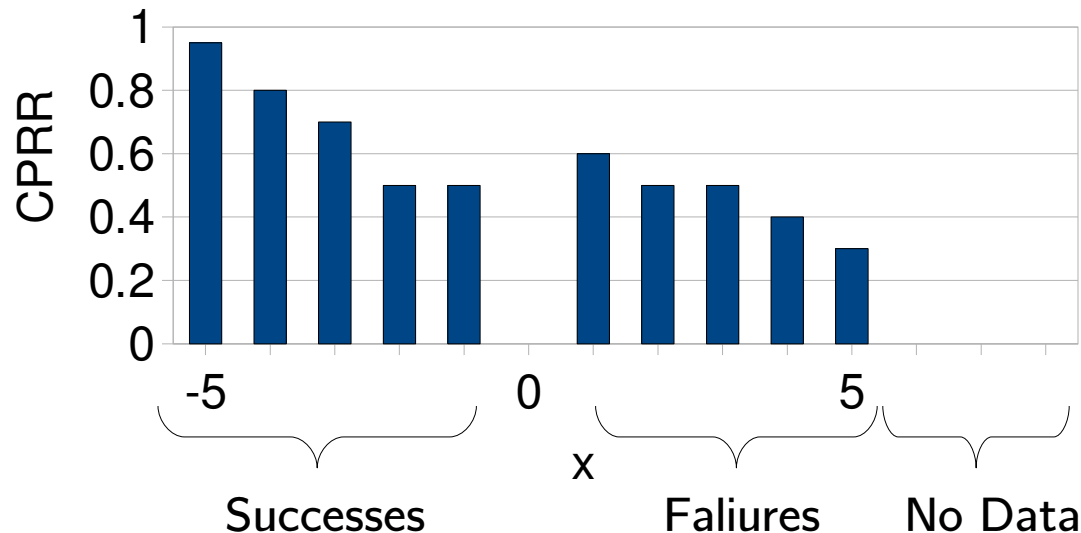
# PRR for Average Value Algorithm

- Maximum absolute error bounded by 28%.



# Conditional Packet Delivery Function (CPDF)

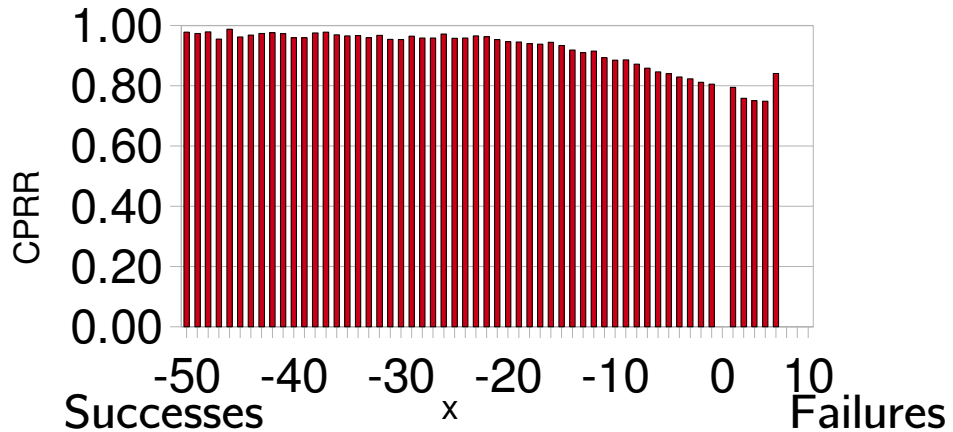
- Considers the conditional packet reception rate (CPRR) after streams of  $|x|$  consecutive receptions for  $x < 0$  or  $x$  consecutive failures for  $x > 0$ .



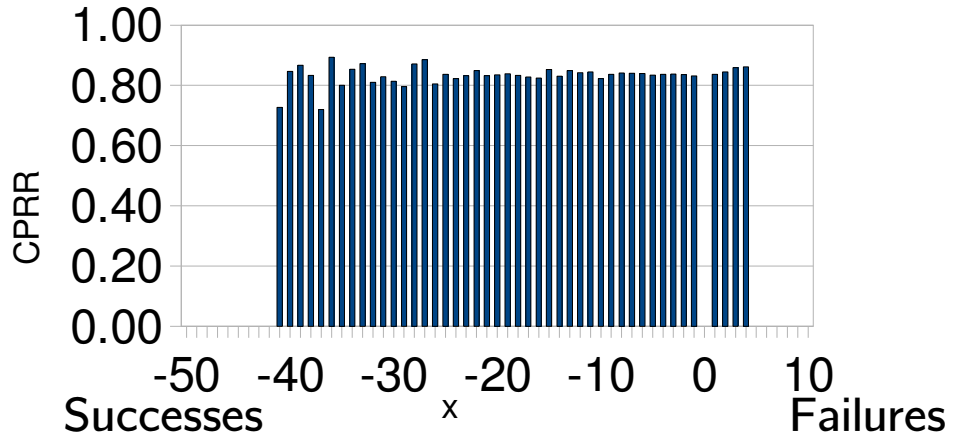
- Kantorovich-Wasserstein Distance measures differences between distributions, including CPDFs.

# CPDF: PRR = 82.5%

Real Signal  
Power



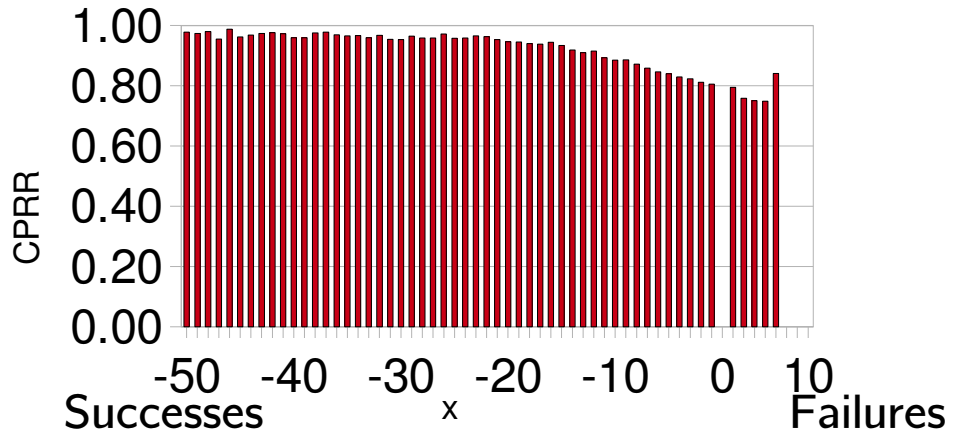
Log Normal  
Shadowing Model



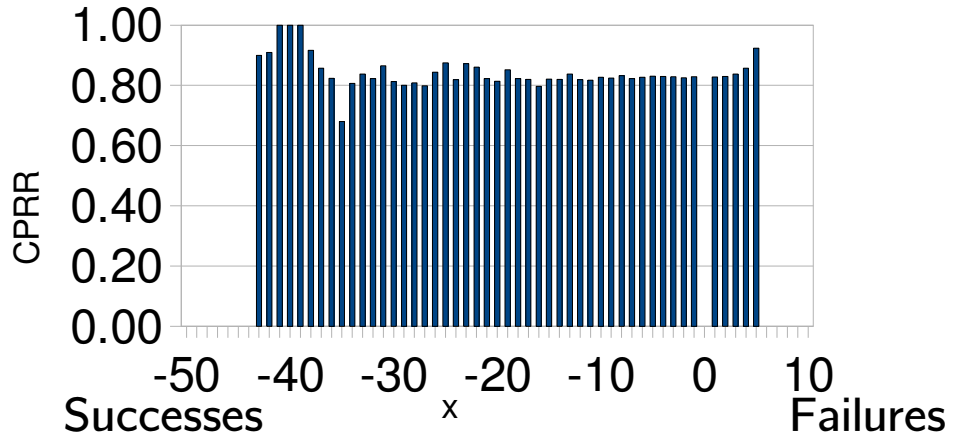
KW Distance = 0.10

# CPDF: PRR = 82.5%

Real Signal  
Power



TOSSIM  
2.0.2

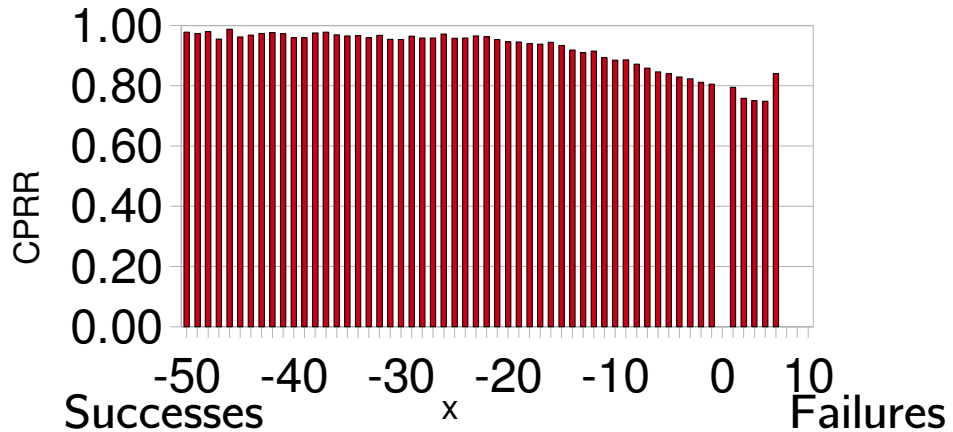


KW Distance = 0.09

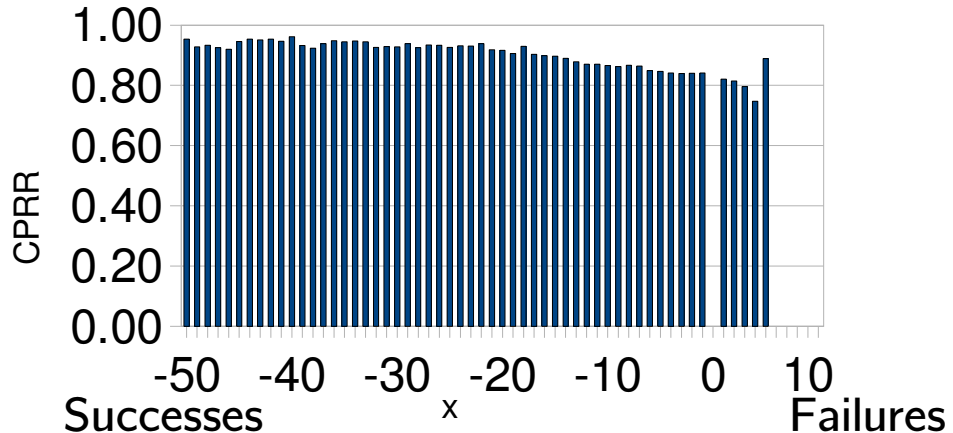


# CPDF: PRR = 82.5%

Real Signal  
Power



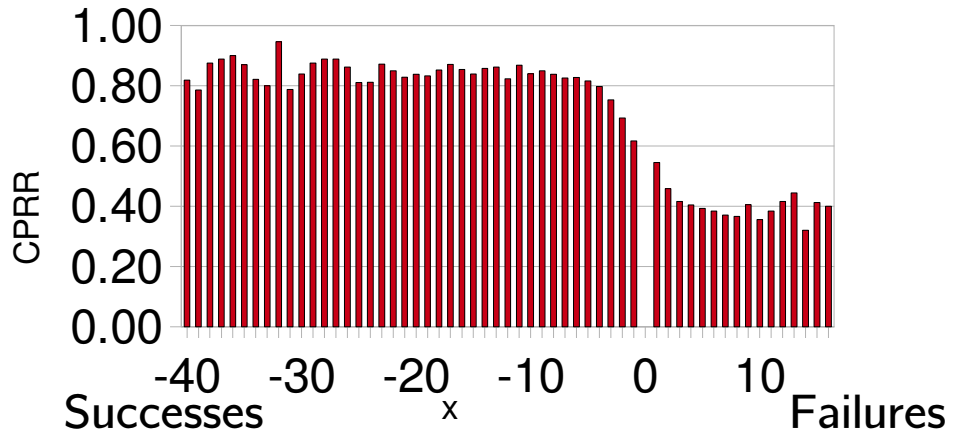
CPM+Expected  
Value PMF



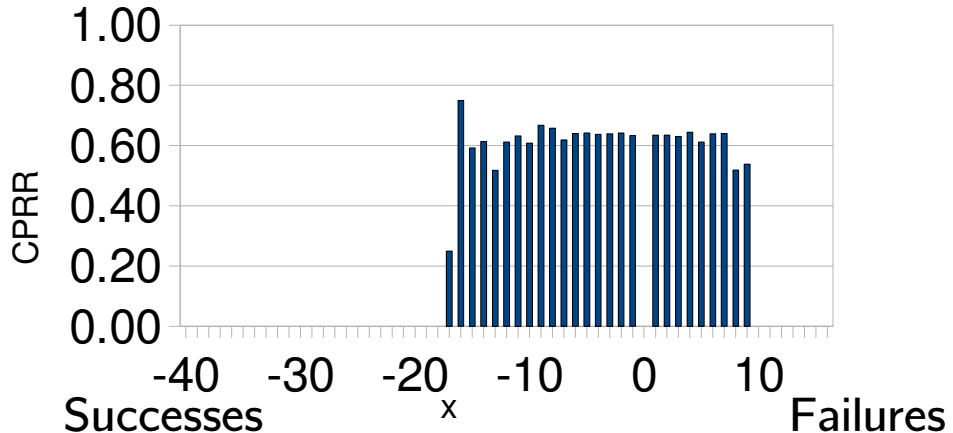
KW Distance = 0.03

# CPDF: PRR = 58.5%

Real Signal  
Power



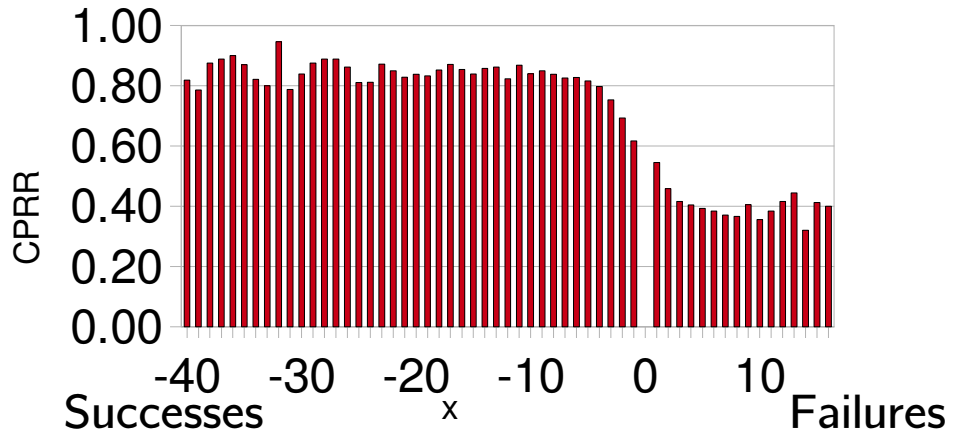
Log Normal  
Shadowing Model



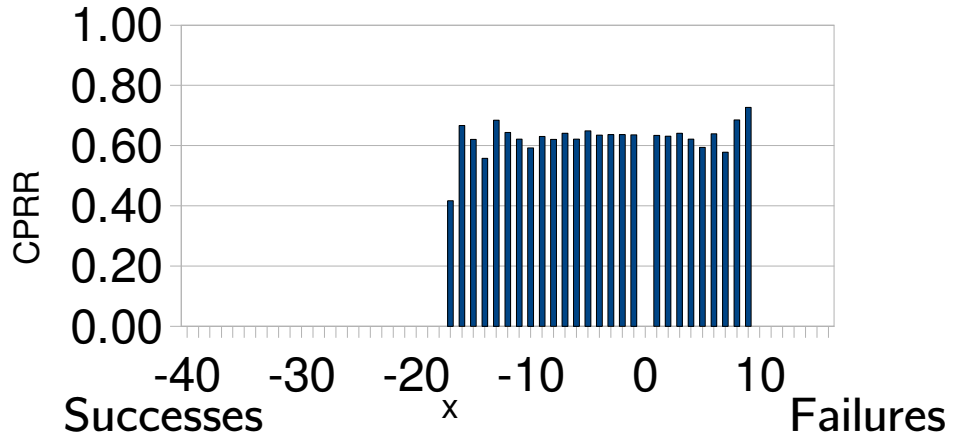
KW Distance = 0.20

# CPDF: PRR = 58.5%

Real Signal  
Power



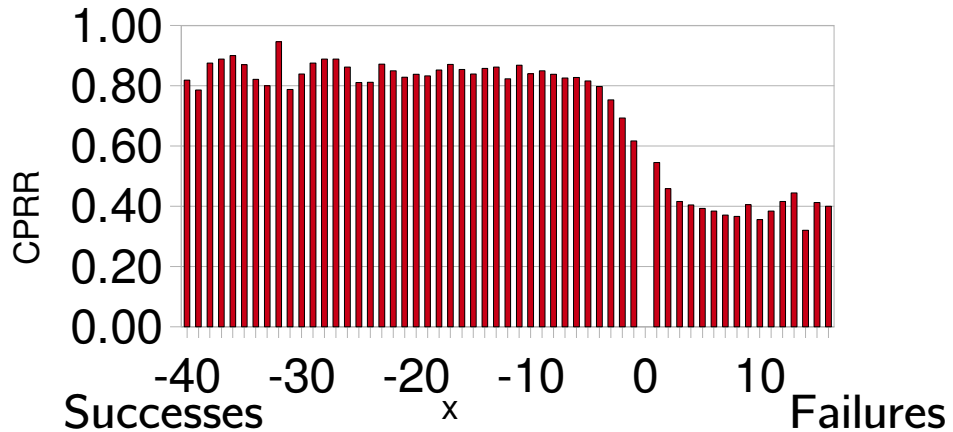
TOSSIM  
2.0.2



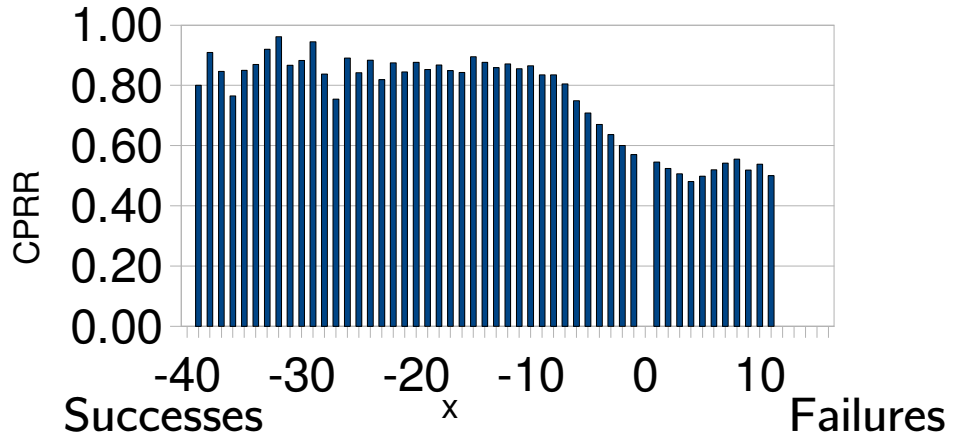
KW Distance = 0.21

# CPDF: PRR = 58.5%

Real Signal  
Power



CPM+Expected  
Value PMF



KW Distance = 0.06

# Outline

---

- Introduction
- Phase correction and signal extrapolation
- Validation and Evaluation
- **Conclusion**

# Conclusions and Future Work

- KW distance  $< 0.1$  for our experiments (substantially reduced as compared to current methods)
- PRR estimated to within 22% (typically to 10%)
- As expected, different assumptions work more effectively for different experiments.
- **Future work:** Development of an automated optimization layer to predict the most reasonable assumptions for a given environment.
- **Future work:** Investigate a signal power model that considers burstiness at many time scales, not just that of an individual packet.

**Thank you.**

---

**Questions?**

**tr76@cornell.edu**

# CPM Model for Trace Histories

- Scan noise trace, keeping a history of size  $k$ .
- For each signature of  $k$  prior noise readings, construct the probability distribution for the next reading.

0 2 1 2 0 2 2 0 0 1 1 1 1 2 0 0 0 2 9 0

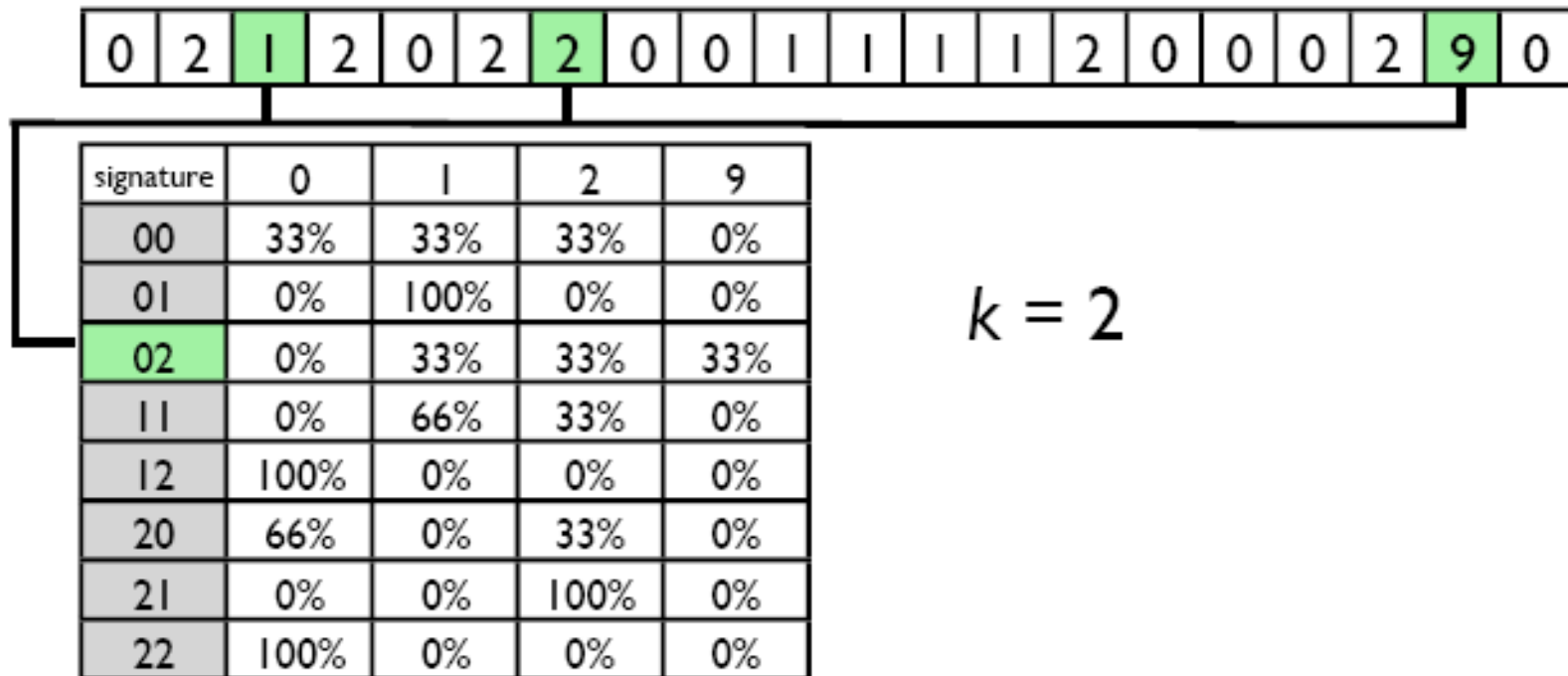
signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$k = 2$

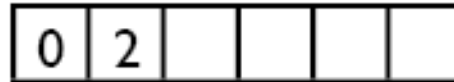


# CPM Model for Trace Histories

- Scan noise trace, keeping a history of size  $k$ .
- For each signature of  $k$  prior noise readings, construct the probability distribution for the next reading.



# CPM Sampling Demo



signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$$k = 2$$

30

# CPM Sampling Demo

0	2	2			
---	---	---	--	--	--

signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$k = 2$

31

# CPM Sampling Demo

0	2	2	0		
---	---	---	---	--	--

signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$k = 2$

32

# CPM Sampling Demo

0	2	2	0	0	
---	---	---	---	---	--

signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$k = 2$

33

# CPM Sampling Demo

0 2 2 0 0 1

signature	0	1	2	9
00	33%	33%	33%	0%
01	0%	100%	0%	0%
02	0%	33%	33%	33%
11	0%	66%	33%	0%
12	100%	0%	0%	0%
20	66%	0%	33%	0%
21	0%	0%	100%	0%
22	100%	0%	0%	0%

$k = 2$

34

# CPM Sampling Result

- Modeled trace is not the same as the experimental trace:

0	2	2	0	0	1
---	---	---	---	---	---

0	2	1	2	0	2	2	0	0	1	1	1	1	2	0	0	0	2	9	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

- This increases the randomness of simulation output and thus decreases the predictability of the simulation.
- This allows for substantial representative simulation.